



Planning and Control of Space Robotic Systems on Orbit

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Motivation

- Space (on-orbit tasks)
 - Hazardous or physically impossible
 - Very costly safety support systems
- A solution: Space robots
- Unique Problems
 - No fixed-base
 - Base-manipulator coupling





Free-floating Space Robots - 1

- Satellite with one or more manipulators
- Free-floating => Base thrusters do not operate.
- A space robot with an N-dof manipulator has N+6 dof.
- N manipulator dof are actuated.
- **Underactuated** system.
- Kinematics and dynamics **reduced** to N equations using *momentum* equations.



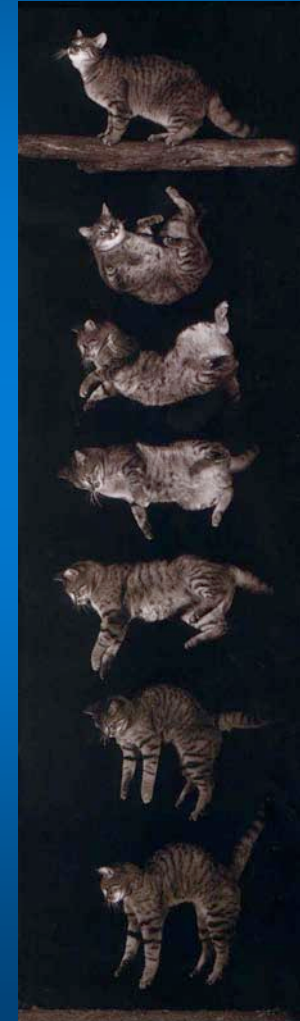
Free-floating Space Robots - 2

- Use reduced kinematics and dynamics (N dof)
- Non-integrable angular momentum conservation must be **appended**
- Nonholonomic behavior:
Spacecraft attitude = $f(\text{manipulator joint-space path})$



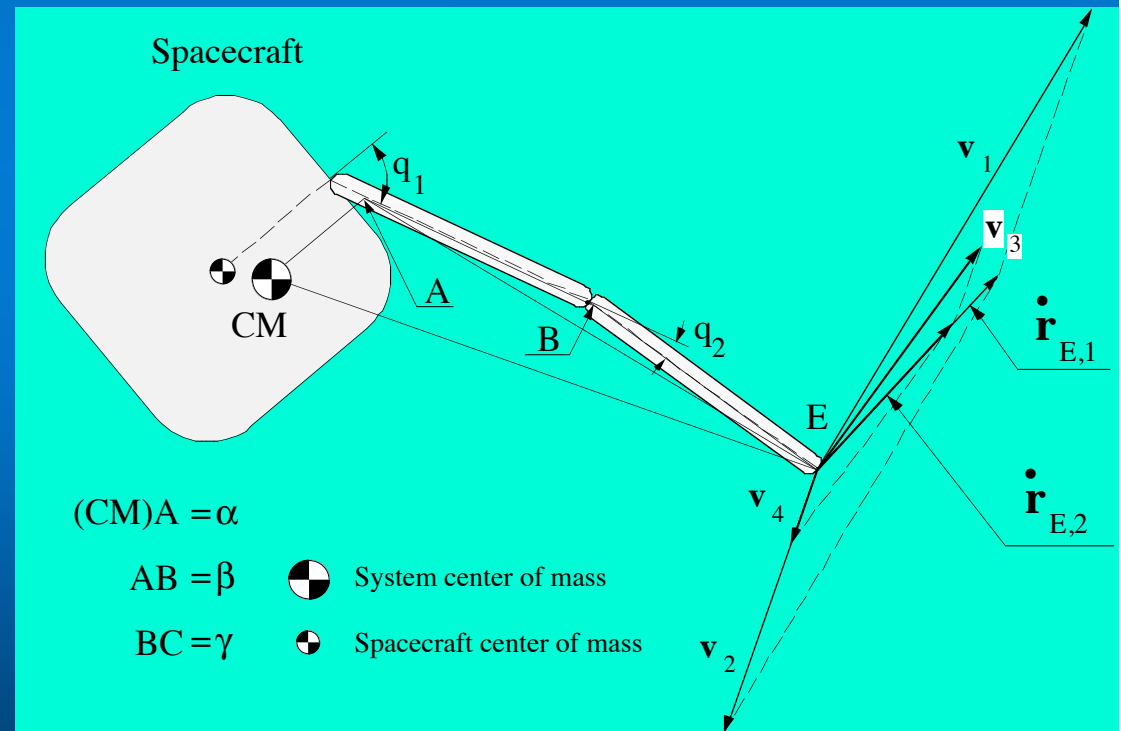
Free-floating Robots Planning

- Can we control a spacecraft's attitude & end-effector position using manipulator motions only?
 - Hard question
 - Astronauts, cats
 - Joint space motions
 - Cartesian space motions & dynamic singularities



Dynamic Singularities - 1

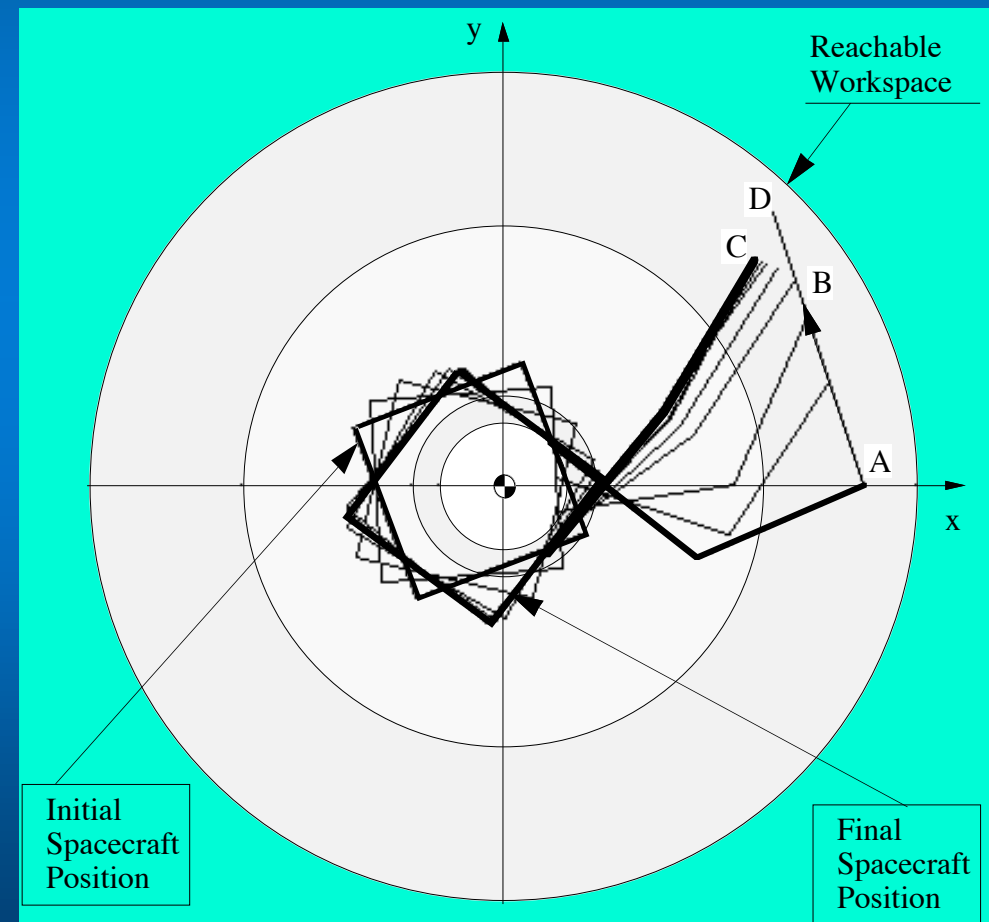
- At a dynamic singularity (shown here)
 - Base motion counteracts end-effector motion
 - Motion dofs are lost
 - Cartesian location singularity is **path dependent**
 - All control algorithms fail there.





Dynamic Singularities - 2

- Move from A to D on a straight line
 - Use a Transpose Jacobian algorithm
 - End-effector moves up to point B
 - At B, a dynamic singularity occurs
 - End-effector moves to point C
 - Cannot recover (Null space)
 - Other algorithms would fail there.



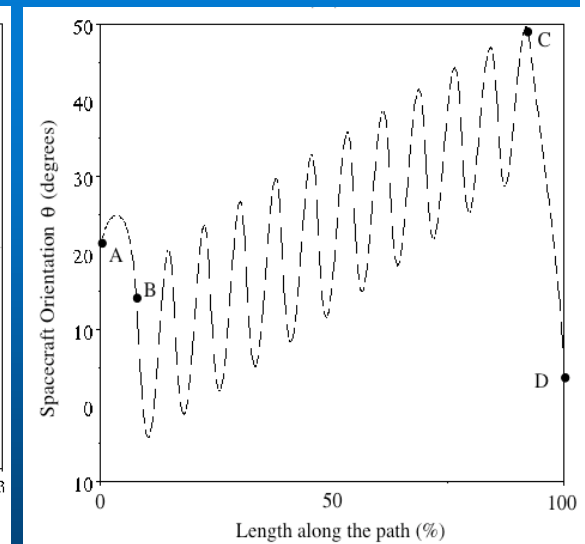
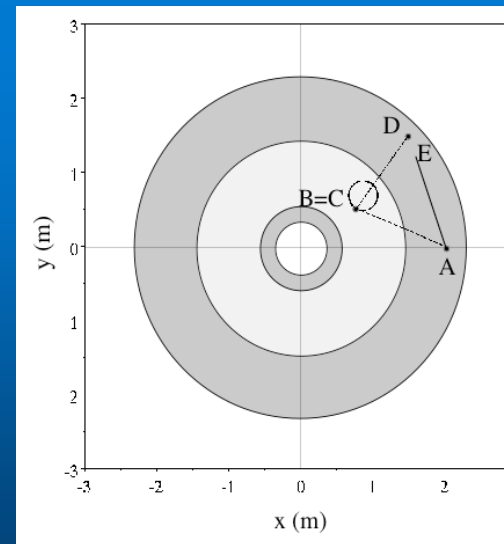


Point to Point Control: Early Solution

- Find a simple path, if any, that will take the end-effector to a desired point, avoiding dynamic singularities

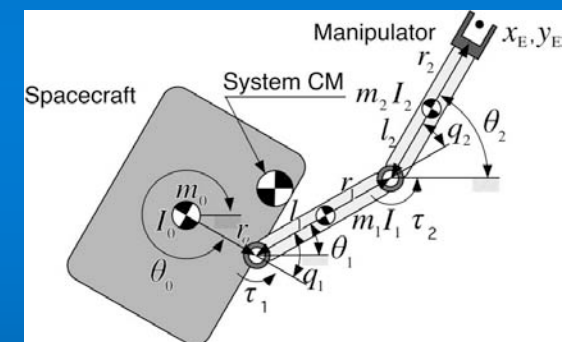
Cyclical Motions

- A→C in PIW, record attitude
- D→C in PIW, record attitude
- Small cyclical motions to match attitudes (Lie)
- **Inexact** computation for number of required cycles
- **Time consuming** & not straightforward



Problem Statement

- Find a simple path, if any, that will take the space robot to a desired configuration
 - in prescribed time,
 - without small cyclical motions,
 - with smooth trajectories, torques,
 - using the actuated manipulator only.





Methodology Outline

- The **key idea** is to use **high order polynomials** as **arguments** in cosines.
- The initial problem is converted to one of satisfying the motion integrals.
- The configuration accessibility is **drastically extended**.
- Free parameters are determined by optimization techniques.
- **At least one path can be obtained**, provided that the desired change in configuration lies between physically permissible limits.



Attitude Permissible Bounds

- A change in manipulator configuration causes a bounded change in base attitude $\Delta\theta_0$

$$d\theta_0 = -\frac{(D_1 + D_2)}{D} dq_1 - \frac{D_2}{D} dq_2 \triangleq g_1(\mathbf{q})dq_1 + g_2(\mathbf{q})dq_2$$

$$\Delta\theta_0 = \int g_1(\mathbf{q})dq_1 + \int g_2(\mathbf{q})dq_2 \triangleq \Delta\theta_{01} + \Delta\theta_{02}$$

where g_1, g_2 are bounded functions of \mathbf{q} .

- Bounds for base attitude change are computed

$$\Delta\theta_{0,\min} < \Delta\theta_0 < \Delta\theta_{0,\max}$$

- If $\Delta\theta_0$ outside the computed range, *no path* exists.



Kinematics - 1

- Base attitude described using ZYX Euler angles (Yaw-Pitch-Roll)

$$\psi_0 = [\theta_1 \quad \theta_2 \quad \theta_3]^T$$

- Euler Angle rates and angular velocity

$$\dot{\psi}_0 = \mathbf{E}^{-1}(\psi_0)^0 \omega_0 = \frac{1}{c_2} \begin{bmatrix} 0 & s_3 & c_3 \\ 0 & c_2 c_3 & -c_2 s_3 \\ c_2 & s_2 s_3 & s_2 c_3 \end{bmatrix}^0 \omega_0$$

q

- Manipulator configuration



Kinematics - 2

- End-effector location/orientation a function of **base attitude and q**
- Cartesian and joint space problem are now equivalent
- Joint space planning NOT subject to dynamic singularities!
- Therefore, plan in joint space.



Dynamics

- Zero external forces and moments
- N Equations of motion

$$\mathbf{H}(\mathbf{q})\ddot{\mathbf{q}} + \mathbf{C}(\mathbf{q}, \dot{\mathbf{q}}) = \boldsymbol{\tau}$$

- Angular momentum

$${}^0\boldsymbol{\omega}_0 = \underbrace{-{}^0\mathbf{D}^{-1}(\mathbf{q}){}^0\mathbf{D}_q(\mathbf{q})}_{\mathbf{F}_1(\mathbf{q})}\dot{\mathbf{q}}$$



Nonholonomic Planning - 1

- Angular momentum (rewritten) $\dot{\boldsymbol{\psi}}_0 = \mathbf{E}^{-1}(\boldsymbol{\psi}_0)\mathbf{F}_1(\mathbf{q})\dot{\mathbf{q}}$
- Path = ? : $(\boldsymbol{\psi}_0^{in}, \mathbf{q}^{in}) \Rightarrow (\boldsymbol{\psi}_0^{fin}, \mathbf{q}^{fin})$
by actuating manipulator joints only.
- Let: $q_i = q_i(t, \mathbf{b}_i)$, $\mathbf{b}_i ((k_i + 1) \times 1)$, $i = 1, \dots, N$
polynomials of order k_i
- Free parameters: $n_f = (k_1 + k_2 + \dots + k_N + N)$
(for N-dof manipulator)



Nonholonomic Planning - 2

- Min #Constraints: $n_c \geq 6N + 3$
 - **Six** per joint (for initial – final position, and zero initial – final velocities & accelerations)
 - Plus at least **three**, for the integrals of motion (the angular momentum conservation equation in three axes)
- Since it must be: $n_f \geq n_c$ we have

$$(k_1 + k_2 + \dots + k_N) \geq 5N + 3$$

$$k_i \geq 5, (i = 1, \dots, N)$$



Nonholonomic Planning - 3

- Let $\mathbf{b} \in \mathbb{R}^k$ the vector containing the remaining free parameters for all \mathbf{b}_i ($i = 1, \dots, N$), after boundary conditions for all joints are satisfied.
- Then we can write $\mathbf{q} = \mathbf{q}(t, \mathbf{b})$ and $\dot{\psi}_0 = \mathbf{F}(\psi_0, \mathbf{b}, t)$
- Free parameters should be **at least three**, i.e. ($k \geq 3$) and satisfy the integrals of motion, i.e.

$$\psi_0^{fin}(\mathbf{b}) = \psi_0^{fin}(des), \text{ or}$$

$$\mathbf{h}(\mathbf{b}) \triangleq \psi_0^{fin}(\mathbf{b}) - \psi_0^{fin}(des) = \mathbf{0}$$

- The problem reduces to determining the unknown vector \mathbf{b} , numerically.



Nonholonomic Planning - 4

- If $k \geq 3$ the vector \mathbf{b} , is determined using optimization techniques, as

$$\|\mathbf{b}\| \rightarrow \min : \mathbf{h}(\mathbf{b}) = \mathbf{0}$$

- Even for $k = 3$ the problem may have multiple solutions (i.e. paths achieving the double goal).
- Approach always yields a path, if the desired change in attitude lies between physically permissible bounds.



Discussion on Planning - 1

- We are mostly interested in finding solution(s) satisfying the equality constraints, rather than finding the global minimum for **b**.
- Additional requirements, i.e.
 - Attitude change maximization
 - Joint limits
 - Obstacle avoidancecan be achieved, by adding more freedom to the end-point path, via the use of higher order polynomials for one or more joints.



Discussion on Planning - 2

- With joint-space trajectories determined, the base attitude is given by integrating $\dot{\psi}_0 = \mathbf{F}(\psi_0, \mathbf{b}, t)$
- Initial and final velocities and accelerations of ψ_0 are necessarily **zero**
- Since the path is defined directly in the joint space, it is always feasible and will never be subject to Dynamic Singularities problems

Planar Example

- Angular momentum

$$D_0(\mathbf{q}) d\theta_0 + D_1(\mathbf{q}) d\theta_1 + D_2(\mathbf{q}) d\theta_2 = 0$$

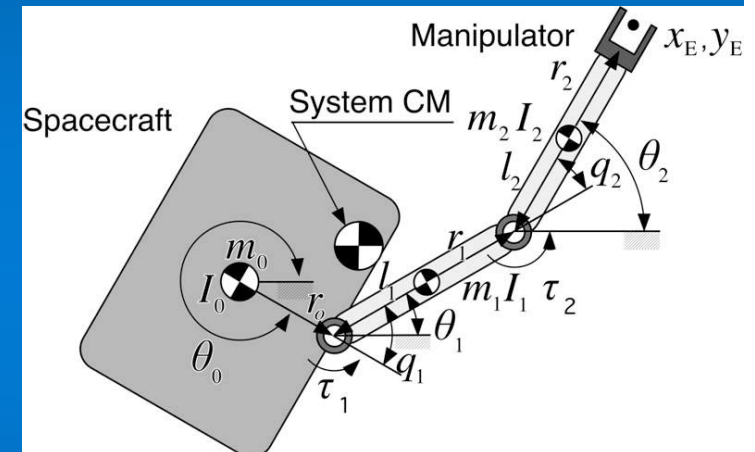
- End-point location

$$x_E = a \cos \theta_0 + b \cos \theta_1 + c \cos \theta_2$$

$$y_E = a \sin \theta_0 + b \sin \theta_1 + c \sin \theta_2$$

- System parameters

Body	l_i (m)	r_i (m)	m_i (Kg)	I_i (Kg.m ²)
0	1.0	0.5	400	66.667
1	0.5	0.5	40	3.33
2	0.5	0.5	30	2.5



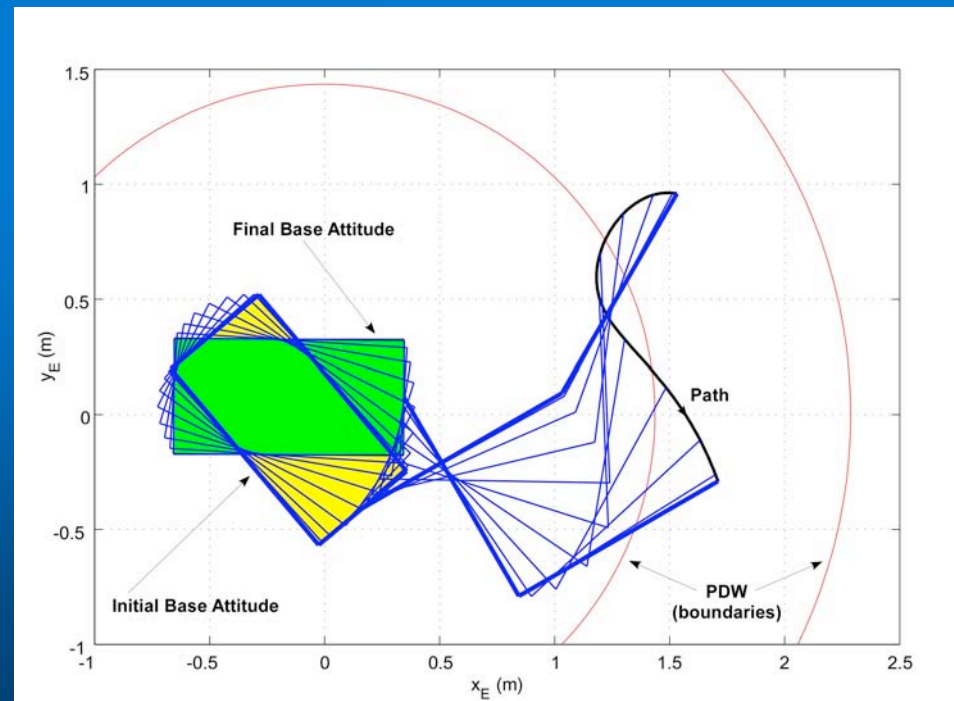
2D: New System Configuration - 1

$$(\theta_0, x_E, y_E)^{in} = (-50^\circ, 1.53m, 0.96m) \xrightarrow{\text{desired}} (\theta_0, x_E, y_E)^{fin} = (0^\circ, 1.71m, -0.29m)$$

$$(\Delta q_1, \Delta q_2) = (-140.0^\circ, 60.0^\circ), \Delta \theta_0 \in (1.4^\circ, 72.2^\circ)$$

$$\Delta \theta_0^{des} = 50^\circ: k_1 = 5, k_2 = 6 \Rightarrow \text{Infinite solutions for } b_{26}(\text{free}). t = 10s.$$

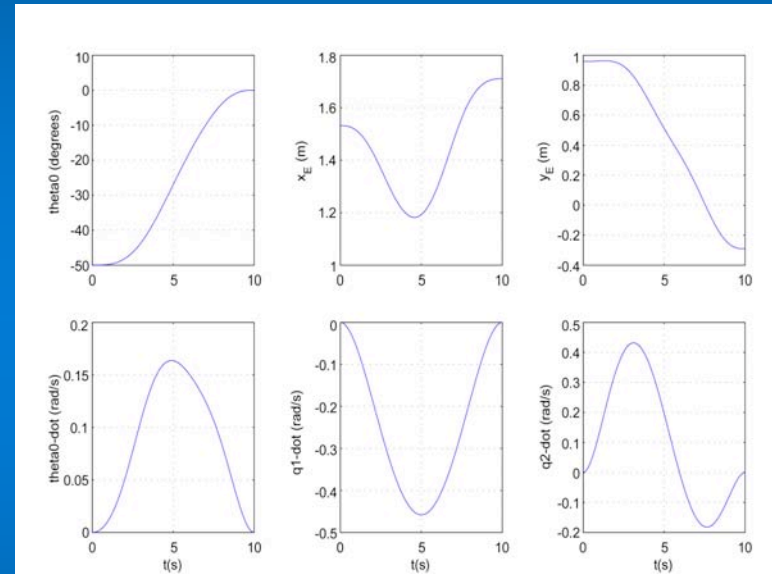
- Using optimization, minimum b_{26} is defined, yielding the shortest path, as shown



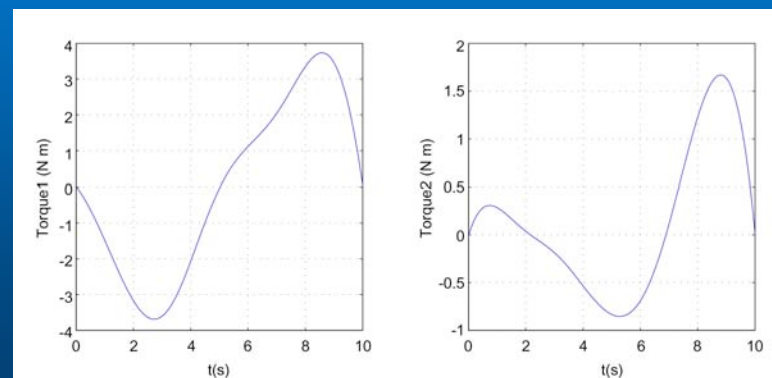


2D: New System Configuration - 2

- Configuration history

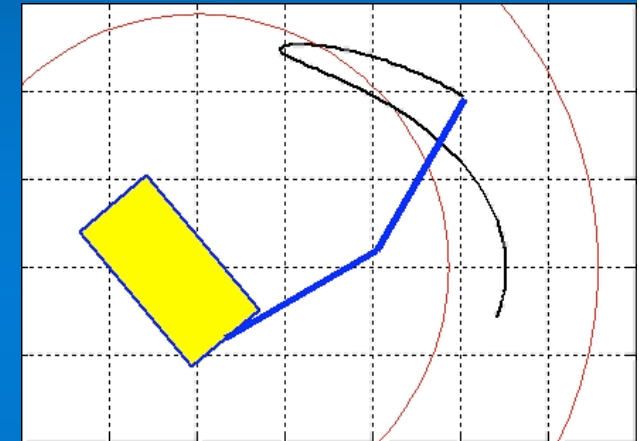
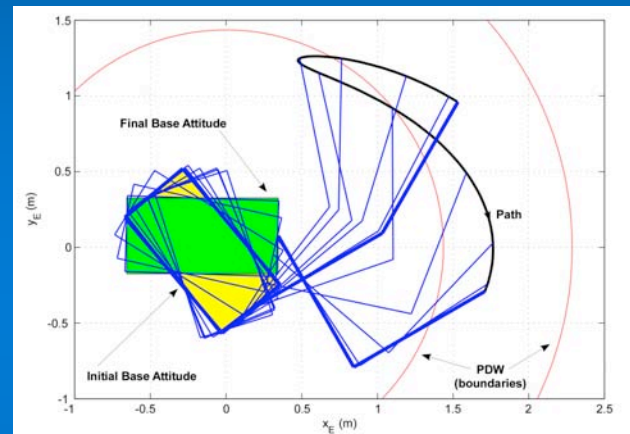


- Actuator torques

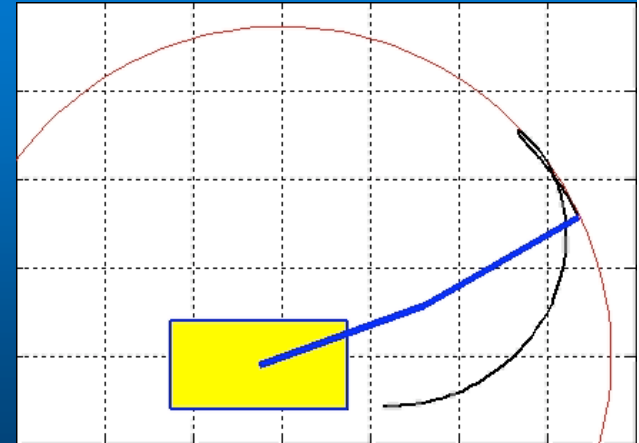
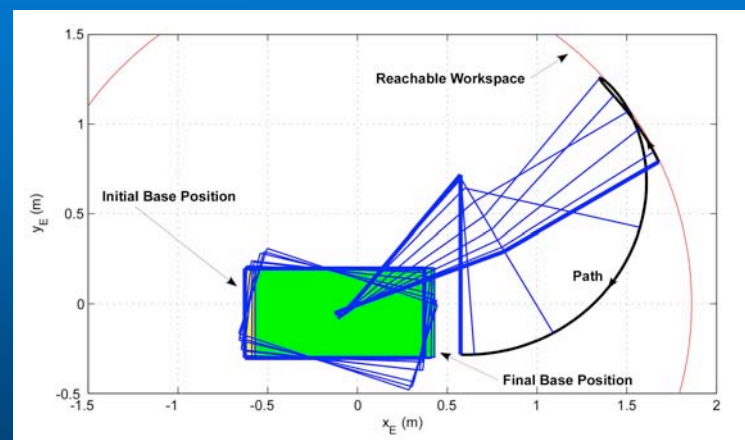


Planning & Control

- Moving to a **new** prescribed **configuration** with two controls



- Moving to a **new point**, keeping the orientation **constant**



Spatial Example

- Base has 6-dof
- 3D manipulator has 3 actuated links (3 dof)
- Total 9 dof

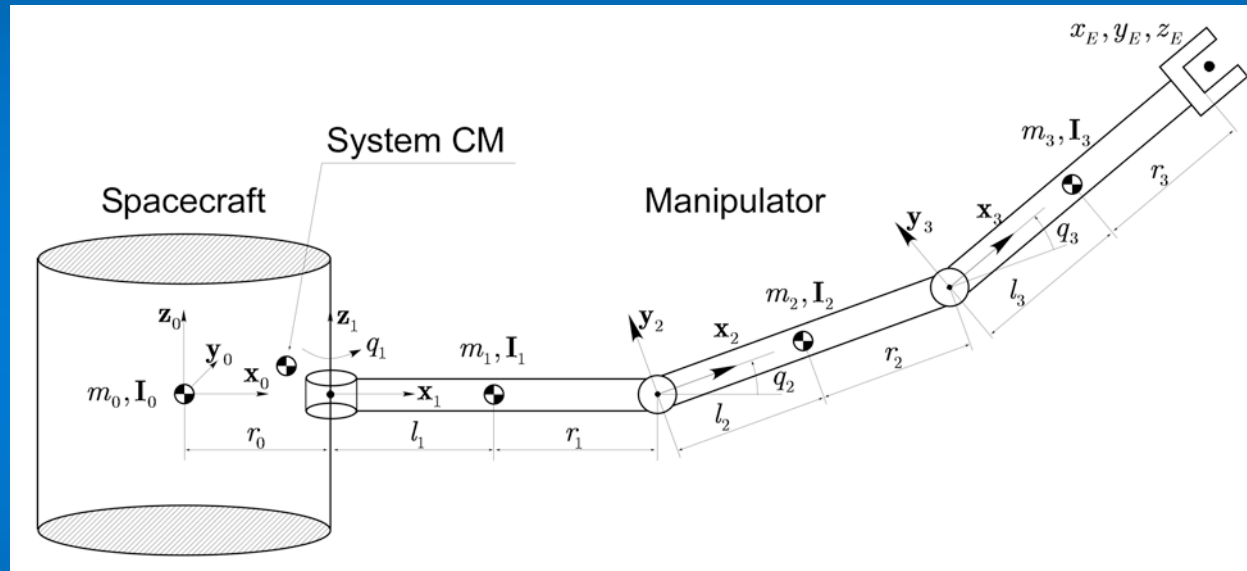


TABLE 2. Spatial System Parameters

Body	l_i [m]	r_i [m]	m_i [kg]	I_{xx}, I_{yy}, I_{zz} [kgm ²]
0	0.5	0.5	400.0	66.7, 66.7, 66.7
1	0.5	0.5	30.0	0, 2.5, 2.5
2	0.5	0.5	30.0	0, 2.5, 2.5
3	0.5	0.5	20.0	0, 1.7, 1.7

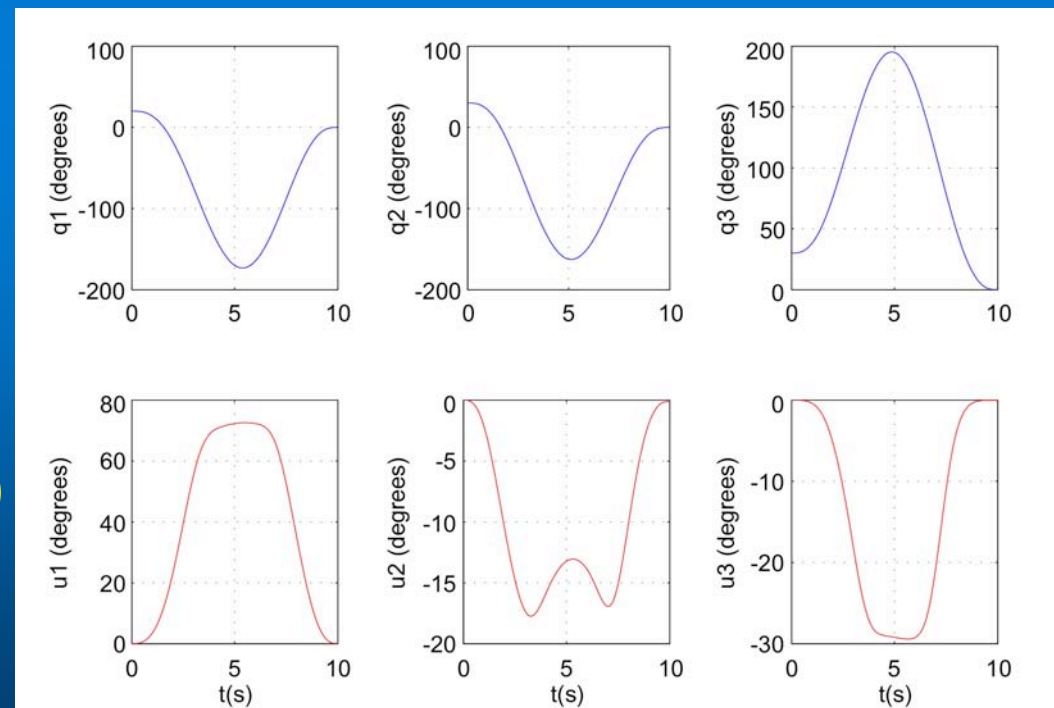


3D: New Endpoint, Same Attitude

$$\psi_0^{fin} = \psi_0^{in}$$

$$(q_1, q_2, q_3)^{in} = (20, 30, 30)^o \xrightarrow{\text{desired}} (q_1, q_2, q_3)^{fin} = (0, 0, 0)^o$$

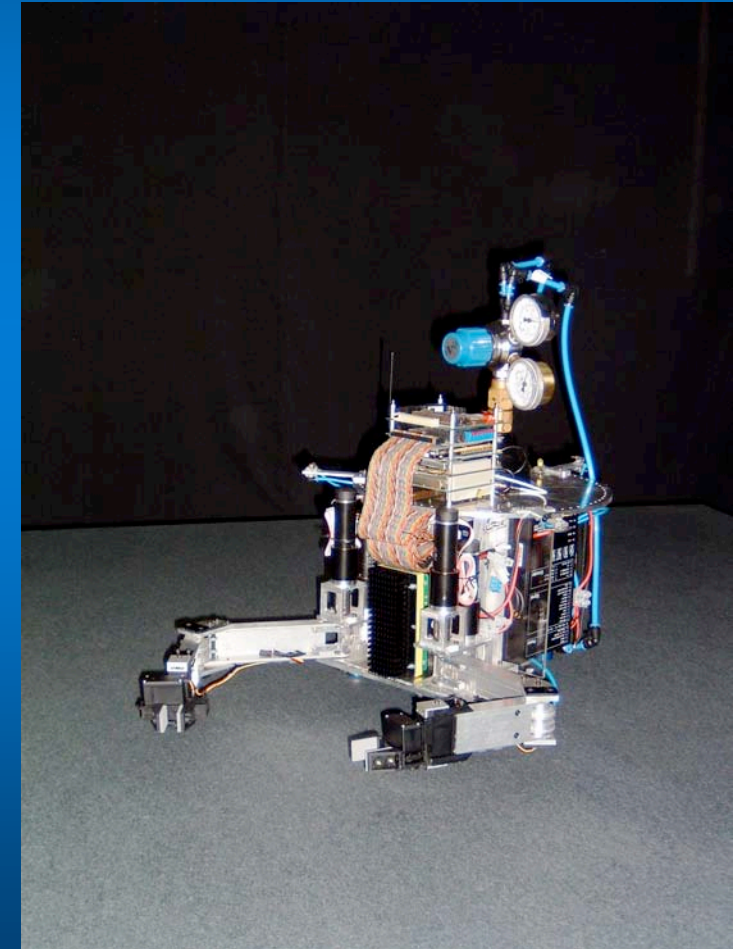
*Joint trajectories and
resulting base attitude
(for $k_1 = 7, k_2 = 6, k_3 = 6$)*





Space Robot Simulator @ NTUA

- Robotic swarms, debris capture, assembly & maintenance tasks
- Two 2 dof manipulators
- 5 μm gap airbearing technology
- Thrust provided by PWM operated solenoid valves
- Fully autonomous, WiFi
- Optoelectronics, encoders, camera sensing
- QNX RTOS @ PC104 deck





Conclusions

- Developed point-to-point planning methods for controlling *both* base attitude and end-effector location
- The *key idea* is to use *high order polynomials* (as arguments in cosines), which drastically extend final configuration accessibility
- Optimization methods allow for easy determination of free parameters
- This approach leads always to a path, provided that the desired change in configuration lies between physically permissible limits
- System smoothly driven to desired configurations in prescribed time